# VIRGINIA STANDARDS OF LEARNING 

Spring 2005 Released Test

# END OF COURSE GEOMETRY 

## CORE 1

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## Geometry Formula Sheet

## Geometric Formulas



Geometric Symbols

| Example | Meaning | Example | Meaning |
| :---: | :---: | :---: | :---: |
| $\angle A$ | angle $A$ | $\overrightarrow{A B}$ | vector $A B$ |
| $\mathrm{m} \angle A$ | measure of angle $A$ | $\downarrow$ | right angle |
| $\stackrel{\rightharpoonup}{A B}$ | line segment $A B$ | $\overleftrightarrow{A B \\|} \overleftrightarrow{C D}$ | Line $A B$ is parallel to line $C D$. |
| $A B$ | measure of line segment $A B$ | $\overleftrightarrow{A B} \perp \overleftrightarrow{C D}$ | Line $A B$ is perpendicular to line $C D$. |
| $\overleftrightarrow{A B}$ | line $A B$ | $\angle A \cong \angle B$ | Angle $A$ is congruent to angle $B$. |
| $\triangle A B C$ | triangle $A B C$ | $\triangle A \sim \triangle B$ | Triangle $A$ is similar to triangle $B$. |
| $\square A B C D$ | rectangle $A B C D$ |  | Similarly marked segments are congruent |
| $\checkmark$ ABCD | parallelogram $A B C D$ | $A D^{\circ}$ | Similarly marked angles are congruent. |

Abbreviations

| Volume | $V$ |
| :--- | :--- |
| Lateral Area | L.A. |
| Total Surface <br> Area | S.A. |
| Area of Base | $B$ |

## Pi

$$
\begin{aligned}
& \pi \approx 3.14 \\
& \pi \approx \frac{22}{7}
\end{aligned}
$$

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## Geometry

## DIRECTIONS

Read and solve each question. Then mark the space on the answer sheet for the best answer.

SAMPLE


If $\triangle A B C$ is similar to $\triangle A D E$, then $A B: A D=$ ?: $A E$. Which replaces the "?" to make the statement true?

A $A C$
B $A E$
C $D E$
D $B C$

1 The measures of some angles are given in the figure.


What is the value of $x$ ?
A 65
B 70
C 80
D 85

2 The figure shows line $l$ intersecting lines $r$ and $s$.


In the figure, $\angle 1$ and $\angle 2$ are -
F alternate interior angles
G alternate exterior angles
H corresponding angles
J consecutive interior angles

3 The Department of Transportation wants to extend the intersecting road across the highway, as indicated by the dotted line.


What should $x$ be to ensure that the intersecting road and the new construction form a straight line?

A $35^{\circ}$
B $55^{\circ}$
C $105^{\circ}$
D $125^{\circ}$

4 The polygon shown is convex.


The sum of its interior angle measures is -

F $900^{\circ}$
G $1,260^{\circ}$
H $1,620^{\circ}$
J $2,520^{\circ}$

5


Which statement would be sufficient to prove that line $l$ is parallel to line $m$ ?

A $\overline{A C} \perp m$
B $\overline{A B} \perp l$
C $\overline{A C} \perp l$
D $\overline{A B} \perp \overline{A C}$

6 In this diagram, line $d$ cuts three lines to form the angles shown.


Which two lines are parallel?
F $a$ and $b$
G $a$ and $c$
H $b$ and $c$
J No lines are parallel.

7 Quadrilateral QRST is placed on a coordinate grid as shown.


What coordinates for $S$ make $Q R S T$ a parallelogram?

A $(8,6)$
B $(8,10)$
C $(12,6)$
D $(12,10)$

8


Which condition will guarantee that line $l$ is parallel to line $m$ ?

F $\angle 1 \cong \angle 3$
G $\angle 1 \cong \angle 6$
H $\angle 6 \cong \angle 5$
J $\angle 3 \cong \angle 5$

9


The drawing shows a compass and straightedge construction of -

A a perpendicular to a given line from a point not on the line
B a perpendicular to a given line at a point on the line
C the bisector of a given angle
D an angle congruent to a given angle


Which point would be on a line perpendicular to $l$ through $T$ ?

F $W$
G $X$
H $Y$
J $Z$


To which point should a line segment from $A$ be drawn so that the resulting figure is a rectangle?

A $W$
B $X$
C $Y$
D $Z$
$12 \Delta X Y Z$ is similar to $\Delta S T R . X Y=6$ and $S T=12$. If the perimeter of $\Delta S T R$ is 38 , then what is the perimeter of $\Delta X Y Z$ ?

F 19
G 38
H 52
J 76

13 Let $p$ represent

$$
\sqrt{11}=z,
$$

and let $q$ represent
$z$ is a rational number.
Which is a representation of the statement below?

If $\sqrt{11}=z$, then $z$ is not a rational number.

A $\sim p \rightarrow \sim q$
B $p \rightarrow q$
C $p \rightarrow \sim q$
D $\sim q \rightarrow \sim p$

14


According to the Venn diagram, which statement is true?

F All isosceles triangles are also equilateral triangles.
G All equilateral triangles are also isosceles triangles.
H Some equilateral triangles are also isosceles triangles.
J No isosceles triangles are equilateral triangles.

15 Which of the following statements represents a valid argument?

A If $a>b$ and $a>c$, then $b>c$.
B If $a>b$ and $b>c$, then $a>c$.
C If $a<b$ and $a<c$, then $c<b$.
D If $a>b$ and $a>c$, then $a>b+c$.

16 Given: $\angle A X Y \cong \angle A B C$

$$
\angle A Y X \cong \angle A C B
$$



Which is a true proportion?
F $\frac{A X}{A B}=\frac{A Y}{A C}=\frac{X Y}{B C}$
G $\frac{A X}{\overline{X B}}=\frac{A Y}{Y C}=\frac{X Y}{B C}$
н $\frac{X B}{A X}=\frac{Y C}{A Y}=\frac{B C}{X Y}$
J $\frac{A X}{A B}=\frac{A C}{A Y}=\frac{X Y}{B C}$

17 Given: $\overline{A D}$ and $\overline{B C}$ intersect at $X$ $\boldsymbol{A X}=\boldsymbol{X B}$ $\boldsymbol{C X}=\boldsymbol{X D}$


Which congruency statement is true?
A $\angle A C X \cong \angle B X D$
B $\angle A C X \cong \angle D X B$
C $\angle A C X \cong \angle B D X$
D $\angle A C X \cong \angle D B X$

18 Which list could not be the measures of lengths of the three sides of a given triangle?

F $5 \mathrm{~cm}, 12 \mathrm{~cm}, 15 \mathrm{~cm}$
G $2 \mathrm{ft}, 6 \mathrm{ft}, 5 \mathrm{ft}$
H $11 \mathrm{mi}, 4 \mathrm{mi}, 12 \mathrm{mi}$
J $12 \mathrm{yd}, 35 \mathrm{yd}, 20 \mathrm{yd}$

19


In the drawing of triangle $X Y Z$, which angle has the least measure?

A All angles have the same measure.
B $\angle X Y Z$
C $\angle Z X Y$
D $\angle X Z Y$

20 If $\mathrm{m} \angle A=65^{\circ}, \mathrm{m} \angle B=15^{\circ}, \mathrm{m} \angle C=100^{\circ}$, which lists the sides of the triangle in order from shortest to longest?

F $\overline{A C}, \overline{A B}, \overline{B C}$
G $\overline{B A}, \overline{B C}, \overline{A C}$
H $\overline{B A}, \overline{A C}, \overline{B C}$
Ј $\overline{A C}, \overline{B C}, \overline{B A}$

21 A windlass is used to pull a boat to the dock. The rope is attached to the boat at a point 7 feet below the level of the windlass.


What is the distance from the boat to the dock when the rope is 25 feet?

A 25 ft
B 24 ft
C 18 ft
D 7 ft

22 The parallelogram has the measurements shown.


Which is closest to the length of the altitude, $h$ ?

F 19.63
G 8.91
H 8.67
J 6.81

23


For the triangle represented by the above drawing, what is the length of $\overline{X Z}$ ?

A $7.5 \sqrt{2}$
B $7.5 \sqrt{3}$
C $15 \sqrt{2}$
D $15 \sqrt{3}$

24


In rectangle $A B C D$, which of the following pairs of segments are not necessarily congruent?
F $\overline{B D}$ and $\overline{A C}$
G $\overline{A B}$ and $\overline{C D}$
H $\overline{B C}$ and $\overline{D C}$
J $\overline{B E}$ and $\overline{C E}$

25 The town plaza in a certain town is a parallelogram. The town's planning committee has decided to build a fountain at the center of the plaza. This sketch shows the corner points when placed on a coordinate grid.


Which coordinates show where the fountain will be located?

A $(2,0.5)$
B $(0.5,2)$
C $(3,1.5)$
D $(1.5,1)$

26 Quadrilateral $A B C D$ is a parallelogram.


Which of the following must be true?
F $\overline{A B} \cong \overline{A D}$
G $\overline{A C} \cong \overline{B D}$
H $\angle A \cong \angle D$
J $\angle B \cong \angle D$
$27 A B C D$ is a rhombus.


What is the measure of $\angle C B D$ ?
A $50^{\circ}$
B $60^{\circ}$
C $70^{\circ}$
D $75^{\circ}$

28 If each interior angle of a regular polygon measures $120^{\circ}$, how many sides does the polygon have?

F 14
G 12
H 8
J 6

29 Which angle measure below is not a possible measure of an exterior angle of a regular polygon?

A $36^{\circ}$
B $40^{\circ}$
C $45^{\circ}$
D $54^{\circ}$


In the figure, what is the measure of $\angle C$ ?

F $70^{\circ}$
G $90^{\circ}$
H $100^{\circ}$
J $110^{\circ}$
$31 \overline{T V}$ is a diameter of circle $Z$.


What is the value of $x$ ?
A 4
B 6
C 8
D 10

32


If $A P=8$ and $P C=4$, what is the measure of $\overline{A B}$, the diameter of this circle?

F 2
G 4
H 6
J 8
$33 \overline{T W}$ is a diameter of circle $X$, and $\overline{T W}$ is parallel to $\overline{U V}$.


If the measure of $\overparen{T U}$ is $25^{\circ}$, what is the degree measure of $\boldsymbol{U V}$ ?

A $115^{\circ}$
B $130^{\circ}$
C $155^{\circ}$
D $210^{\circ}$

34 This is a scale drawing of a tent where 1 centimeter represents 0.5 meter.


What is the height of the tent at its highest point?

F 10 m
G 5 m
H 3 m
J 2.5 m

35


Which represents a two-dimensional view from directly above the figure?


B


C


D


36 To the nearest gallon, what is the volume of a cylindrical water heater 1.4 feet in diameter and 4 feet tall? ( 1 cubic foot $=7.48$ gallons)

F $\quad 34 \mathrm{gal}$
G 46 gal
H 59 gal
J 132 gal

37 A spherical paintball measures 1.5 centimeters in diameter. Approximately how much paint is in it?

A $1.77 \mathrm{~cm}^{3}$
B $7.07 \mathrm{~cm}^{3}$
C $9.42 \mathrm{~cm}^{3}$
D $14.13 \mathrm{~cm}^{3}$

38


Which proportion can be used to find the value of $\overline{P R}$ if $\triangle X M Q$ is similar to $\Delta P R S ?$

F $\frac{20}{15}=\frac{14}{P R}$

G $\frac{10}{5}=\frac{7}{P R}$

H $\frac{14}{20}=\frac{15}{P R}$

J $\frac{15}{20}=\frac{14}{P R}$

39 When standing upright, Gary knows his eyes are 6 feet above ground level. To determine the depth of a well, he stands in the position shown.


Using the given measures, how deep is the well?

A 12 ft
B 14 ft
C 16 ft
D 18 ft

40


The coordinates of the midpoint of $\overline{A B}$ are -

F $(5,3)$
G $(-5,3)$
H $(2,5)$
J $(-2,5)$

41 Parallelogram $A B C D$ is placed on a coordinate grid as shown.


What is the approximate length of diagonal $\overline{A C}$ ?

A 3.0 units
B 5.4 units
C 9.0 units
D 10.6 units

42


Triangle $\boldsymbol{A}^{\prime} \boldsymbol{B}^{\prime} \boldsymbol{C}^{\prime}$ is -
F a translation of triangle $A B C$ across the $y$-axis
G a $90^{\circ}$ clockwise rotation of triangle $A B C$ about the origin
H a reflection of triangle $A B C$ across the $y$-axis
$J$ a reflection of triangle $A B C$ across the $x$-axis

43 How many different lines of symmetry does a square have?

A 1
B 2
C 3
D 4

44


Which is most likely the slope of the line graphed?

F $\quad-4$

G $\quad-\frac{3}{2}$
H $\quad-\frac{2}{3}$

J 4


Hexagon $A B C D E F$ is apparently symmetric with respect to -

A point $P$ only
B line $m$ only
C line $l$ only
D both lines $l$ and $m$ only

Answer Key

| Test Sequence Number | Correct Answer | Reporting Category | Reporting Category Description |
| :---: | :---: | :---: | :---: |
| 1 | B | 001 | Lines and Angles |
| 2 | H | 001 | Lines and Angles |
| 3 | B | 001 | Lines and Angles |
| 4 | F | 001 | Lines and Angles |
| 5 | B | 001 | Lines and Angles |
| 6 | H | 001 | Lines and Angles |
| 7 | C | 001 | Lines and Angles |
| 8 | J | 001 | Lines and Angles |
| 9 | C | 001 | Lines and Angles |
| 10 | H | 001 | Lines and Angles |
| 11 | B | 001 | Lines and Angles |
| 12 | F | 002 | Triangles and Logic |
| 13 | C | 002 | Triangles and Logic |
| 14 | G | 002 | Triangles and Logic |
| 15 | B | 002 | Triangles and Logic |
| 16 | F | 002 | Triangles and Logic |
| 17 | C | 002 | Triangles and Logic |
| 18 | J | 002 | Triangles and Logic |
| 19 | D | 002 | Triangles and Logic |
| 20 | J | 002 | Triangles and Logic |
| 21 | B | 002 | Triangles and Logic |
| 22 | G | 002 | Triangles and Logic |
| 23 | C | 002 | Triangles and Logic |
| 24 | H | 003 | Polygons and Circles |
| 25 | A | 003 | Polygons and Circles |
| 26 | J | 003 | Polygons and Circles |
| 27 | C | 003 | Polygons and Circles |
| 28 | J | 003 | Polygons and Circles |
| 29 | D | 003 | Polygons and Circles |
| 30 | F | 003 | Polygons and Circles |
| 31 | C | 003 | Polygons and Circles |
| 32 | H | 003 | Polygons and Circles |
| 33 | B | 003 | Polygons and Circles |
| 34 | J | 004 | Three-Dimensional Figures |
| 35 | B | 004 | Three-Dimensional Figures |
| 36 | G | 004 | Three-Dimensional Figures |
| 37 | A | 004 | Three-Dimensional Figures |
| 38 | F | 004 | Three-Dimensional Figures |
| 39 | D | 004 | Three-Dimensional Figures |
| 40 | J | 005 | Coordinate Relations and Transformations |
| 41 | B | 005 | Coordinate Relations and Transformations |
| 42 | F | 005 | Coordinate Relations and Transformations |
| 43 | D | 005 | Coordinate Relations and Transformations |
| 44 | H | 005 | Coordinate Relations and Transformations |
| 45 | B | 005 | Coordinate Relations and Transformations |

