VIRGINIA STANDARDS OF LEARNING

Spring 2005 Released Test

END OF COURSE GEOMETRY

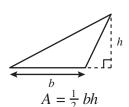
CORE 1

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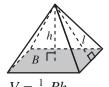
Geometry Formula Sheet

Geometric Formulas



$$A = \frac{1}{2} h(b_1 + b_2)$$

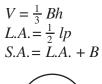




$$V = Bh$$

$$L.A. = hp$$

$$S.A. = L.A. + 2B$$









$$A = lw$$
$$p = 2(l + w)$$

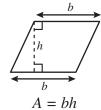


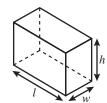
$$V = \pi r^2 h$$

$$L.A. = 2\pi r h$$

$$S.A. = 2\pi r (h + r)$$











$$V = lwh$$

S.A. = $2lw + 2lh + 2wh$

 $V = \frac{1}{3} \pi r^2 h$ $L.A. = \pi r l$ $S.A. = \pi r (l + r)$

Geometric Symbols

Example	Meaning
$\angle A$	angle A
m∠A	measure of angle A
\overline{AB}	line segment AB
AB	measure of line segment AB
\overrightarrow{AB}	line AB
$\triangle ABC$	triangle <i>ABC</i>
\square ABCD	rectangle ABCD
∠ZABCD	parallelogram ABCD

Example	Meaning
\overrightarrow{AB}	vector AB
	right angle
$\overrightarrow{AB} \parallel \overrightarrow{CD}$	Line <i>AB</i> is parallel to line <i>CD</i> .
$\overrightarrow{AB}\bot\overrightarrow{CD}$	Line AB is perpendicular to line CD .
$\angle A \cong \angle B$	Angle A is congruent to angle B .
$\triangle A \sim \triangle B$	Triangle A is similar to triangle B .
	Similarly marked segments are congruent.
	Similarly marked angles are congruent.

Abbreviations

Volume	V
Lateral Area	L.A.
Total Surface Area	S.A.
Area of Base	В

Ρi

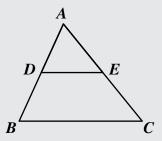
 $\pi\approx 3.14$ $\pi \approx \frac{22}{7}$

Geometry

DIRECTIONS

Read and solve each question. Then mark the space on the answer sheet for the best answer.

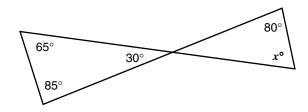
SAMPLE



If $\triangle ABC$ is similar to $\triangle ADE$, then AB:AD=?:AE. Which replaces the "?" to make the statement true?

- \mathbf{A} AC
- \mathbf{B} AE
- \mathbf{C} DE
- \mathbf{D} BC

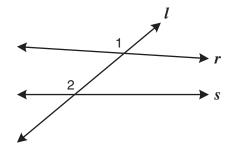
1 The measures of some angles are given in the figure.



What is the value of x?

- **A** 65
- **B** 70
- **c** 80
- **D** 85

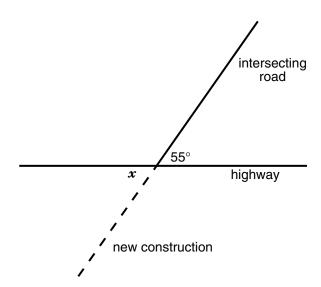
2 The figure shows line l intersecting lines r and s.



In the figure, $\angle 1$ and $\angle 2$ are —

- F alternate interior angles
- G alternate exterior angles
- H corresponding angles
- J consecutive interior angles

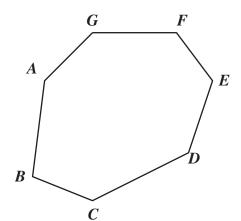
3 The Department of Transportation wants to extend the intersecting road across the highway, as indicated by the dotted line.



What should x be to ensure that the intersecting road and the new construction form a straight line?

- **A** 35°
- \mathbf{B} 55°
- \mathbf{C} 105°
- **D** 125°

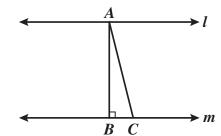
4 The polygon shown is convex.



The sum of its interior angle measures is —

- **F** 900°
- $G 1,260^{\circ}$
- н 1,620°
- **J** $2,520^{\circ}$

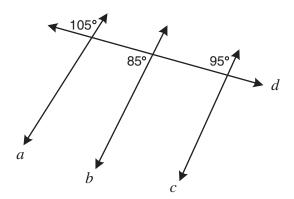
5



Which statement would be sufficient to prove that line l is parallel to line m?

- **A** $\overline{AC} \perp m$
- **B** $\overline{AB} \perp l$
- \mathbf{C} $\overline{AC} \perp l$
- **D** $\overline{AB} \perp \overline{AC}$

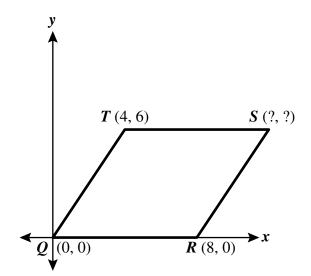
6 In this diagram, line d cuts three lines to form the angles shown.



Which two lines are parallel?

- \mathbf{F} a and b
- \mathbf{G} a and c
- \mathbf{H} b and c
- J No lines are parallel.

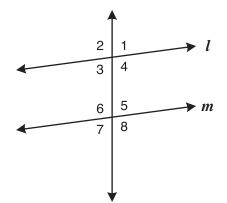
7 Quadrilateral *QRST* is placed on a coordinate grid as shown.



What coordinates for S make QRST a parallelogram?

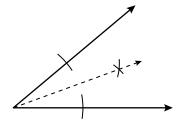
- **A** (8, 6)
- **B** (8, 10)
- **c** (12, 6)
- **D** (12, 10)

8



Which condition will guarantee that line l is parallel to line m?

- $\mathbf{F} \quad \angle 1 \cong \angle 3$
- $\mathbf{G} \quad \angle \mathbf{1} \cong \angle \mathbf{6}$
- **H** $\angle 6 \cong \angle 5$
- \mathbf{J} $\angle 3 \cong \angle 5$



The drawing shows a compass and straightedge construction of —

- A a perpendicular to a given line from a point not on the line
- **B** a perpendicular to a given line at a point on the line
- C the bisector of a given angle
- D an angle congruent to a given angle

10



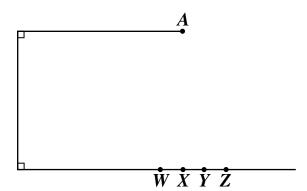
 $\boldsymbol{X} \bullet$



Which point would be on a line perpendicular to l through T?

- \mathbf{F} W
- $\mathbf{G} X$
- $\mathbf{H} Y$
- \mathbf{J} Z

11



To which point should a line segment from A be drawn so that the resulting figure is a rectangle?

- \mathbf{A} W
- $\mathbf{B} X$
- \mathbf{C} Y
- \mathbf{p} Z
- 12 ΔXYZ is similar to ΔSTR . XY=6 and ST=12. If the perimeter of ΔSTR is 38, then what is the perimeter of ΔXYZ ?
 - **F** 19
 - **G** 38
 - **H** 52
 - **J** 76

13 Let *p* represent

$$\sqrt{11}=z,$$

and let q represent

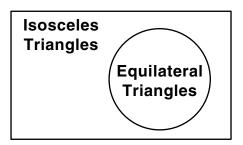
z is a rational number.

Which is a representation of the statement below?

If $\sqrt{11} = z$, then z is not a rational number.

- **A** $\sim p \rightarrow \sim q$
- $\mathbf{B} \quad p \to q$
- $\mathbf{C} \quad p \to \sim q$
- $\mathbf{D} \sim q \rightarrow \sim p$

14



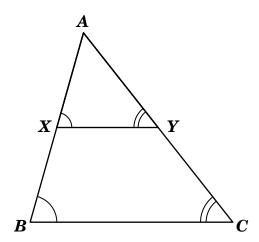
According to the Venn diagram, which statement is true?

- **F** All isosceles triangles are also equilateral triangles.
- G All equilateral triangles are also isosceles triangles.
- H Some equilateral triangles are also isosceles triangles.
- J No isosceles triangles are equilateral triangles.

15 Which of the following statements represents a valid argument?

- **A** If a > b and a > c, then b > c.
- **B** If a > b and b > c, then a > c.
- C If a < b and a < c, then c < b.
- **D** If a > b and a > c, then a > b + c.

16 Given: $\angle AXY \cong \angle ABC$ $\angle AYX \cong \angle ACB$



Which is a true proportion?

$$\mathbf{F} \quad \frac{AX}{AB} = \frac{AY}{AC} = \frac{XY}{BC}$$

$$\mathbf{G} \quad \frac{AX}{XB} = \frac{AY}{YC} = \frac{XY}{BC}$$

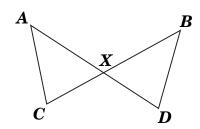
$$\mathbf{H} \quad \frac{XB}{AX} = \frac{YC}{AY} = \frac{BC}{XY}$$

$$\mathbf{J} \quad \frac{AX}{AB} = \frac{AC}{AY} = \frac{XY}{BC}$$

17 Given: \overline{AD} and \overline{BC} intersect at X

$$AX = XB$$

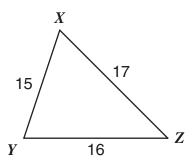
$$CX = XD$$



Which congruency statement is true?

- **A** $\angle ACX \cong \angle BXD$
- **B** $\angle ACX \cong \angle DXB$
- \mathbf{C} $\angle ACX \cong \angle BDX$
- **D** $\angle ACX \cong \angle DBX$
- 18 Which list could *not* be the measures of lengths of the three sides of a given triangle?
 - F 5 cm, 12 cm, 15 cm
 - G 2 ft, 6 ft, 5 ft
 - H 11 mi, 4 mi, 12 mi
 - J 12 yd, 35 yd, 20 yd

19

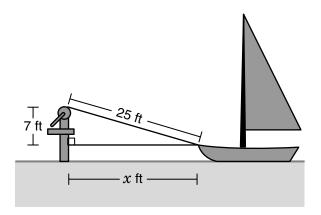


In the drawing of triangle XYZ, which angle has the least measure?

- A All angles have the same measure.
- \mathbf{B} $\angle XYZ$
- \mathbf{C} $\angle ZXY$
- \mathbf{D} $\angle XZY$
- 20 If $m\angle A = 65^{\circ}$, $m\angle B = 15^{\circ}$, $m\angle C = 100^{\circ}$, which lists the sides of the triangle in order from shortest to longest?
 - \mathbf{F} \overline{AC} , \overline{AB} , \overline{BC}
 - $G \overline{BA}, \overline{BC}, \overline{AC}$
 - н \overline{BA} , \overline{AC} , \overline{BC}
 - **J** \overline{AC} , \overline{BC} , \overline{BA}

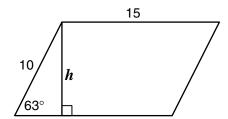
7

21 A windlass is used to pull a boat to the dock. The rope is attached to the boat at a point 7 feet below the level of the windlass.



What is the distance from the boat to the dock when the rope is 25 feet?

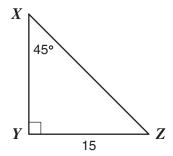
- **A** 25 ft
- **B** 24 ft
- **c** 18 ft
- **D** 7 ft
- 22 The parallelogram has the measurements shown.



Which is closest to the length of the altitude, h?

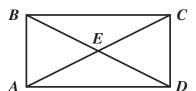
- **F** 19.63
- G 8.91
- н 8.67
- **J** 6.81

23



For the triangle represented by the above drawing, what is the length of \overline{XZ} ?

- $\mathbf{A} \quad 7.5\sqrt{2}$
- **B** $7.5\sqrt{3}$
- $\mathbf{C} \quad 15\sqrt{2}$
- **D** $15\sqrt{3}$
- **24**

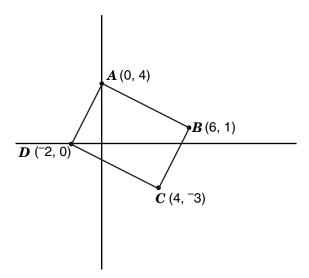


In rectangle *ABCD*, which of the following pairs of segments are *not* necessarily congruent?

- **F** \overline{BD} and \overline{AC}
- **G** \overline{AB} and \overline{CD}
- **H** \overline{BC} and \overline{DC}
- \mathbf{J} \overline{BE} and \overline{CE}

8

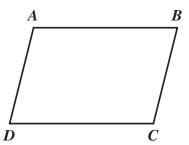
25 The town plaza in a certain town is a parallelogram. The town's planning committee has decided to build a fountain at the center of the plaza. This sketch shows the corner points when placed on a coordinate grid.



Which coordinates show where the fountain will be located?

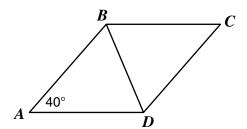
- **A** (2, 0.5)
- \mathbf{B} (0.5, 2)
- **C** (3, 1.5)
- **D** (1.5, 1)

26 Quadrilateral ABCD is a parallelogram.



Which of the following must be true?

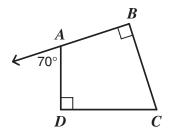
- $\mathbf{F} \quad \overline{AB} \cong \overline{AD}$
- \mathbf{G} $\overline{AC} \cong \overline{BD}$
- **H** $\angle A \cong \angle D$
- **J** $\angle B \cong \angle D$
- 27 ABCD is a rhombus.



What is the measure of $\angle CBD$?

- A 50°
- **B** 60°
- **c** 70°
- **D** 75°

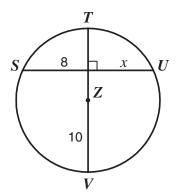
- 28 If each interior angle of a regular polygon measures 120°, how many sides does the polygon have?
 - **F** 14
 - **G** 12
 - **H** 8
 - **J** 6
- 29 Which angle measure below is *not* a possible measure of an exterior angle of a regular polygon?
 - **A** 36°
 - **B** 40°
 - C 45°
 - **D** 54°



In the figure, what is the measure of $\angle C$?

- \mathbf{F} 70°
- \mathbf{G} 90°
- **н** 100°
- J 110°

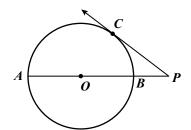
31 \overline{TV} is a diameter of circle Z.



What is the value of x?

- **A** 4
- **B** 6
- **c** 8
- **D** 10

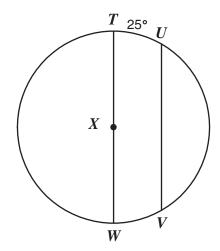
32



If AP = 8 and PC = 4, what is the measure of \overline{AB} , the *diameter* of this circle?

- **F** 2
- **G** 4
- н 6
- **J** 8

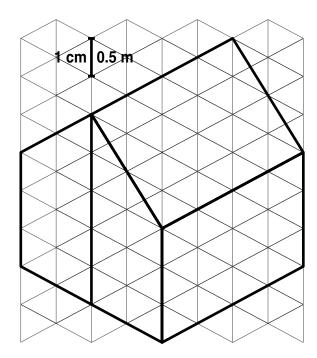
33 \overline{TW} is a diameter of circle X, and \overline{TW} is parallel to \overline{UV} .



If the measure of \widehat{TU} is 25°, what is the degree measure of \widehat{UV} ?

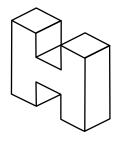
- **A** 115°
- **B** 130°
- C 155°
- **D** 210°

34 This is a scale drawing of a tent where 1 centimeter represents 0.5 meter.

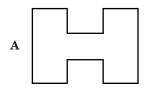


What is the height of the tent at its highest point?

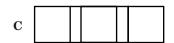
- **F** 10 m
- **G** 5 m
- **H** 3 m
- J 2.5 m

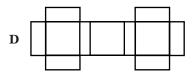


Which represents a two-dimensional view from directly above the figure?









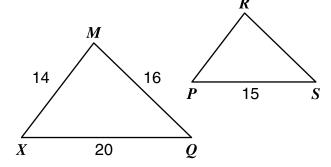
36 To the nearest gallon, what is the volume of a cylindrical water heater 1.4 feet in diameter and 4 feet tall? (1 cubic foot = 7.48 gallons)

- **F** 34 gal
- **G** 46 gal
- **H** 59 gal
- **J** 132 gal

37 A spherical paintball measures
1.5 centimeters in diameter.
Approximately how much paint is in
i+2

- **A** 1.77 cm^3
- **B** 7.07 cm^3
- C 9.42 cm³
- **D** 14.13 cm^3

38



Which proportion can be used to find the value of \overline{PR} if ΔXMQ is similar to ΔPRS ?

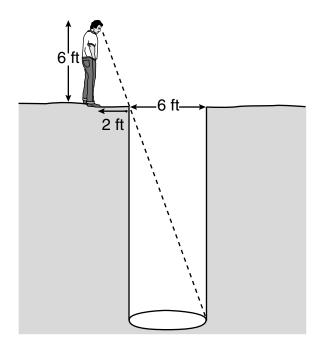
$$\mathbf{F} \quad \frac{20}{15} = \frac{14}{PR}$$

$$\mathbf{G} \quad \frac{10}{5} = \frac{7}{PR}$$

$$\mathbf{H} \quad \frac{14}{20} = \frac{15}{PR}$$

$$\mathbf{J} \quad \frac{15}{20} = \frac{14}{PR}$$

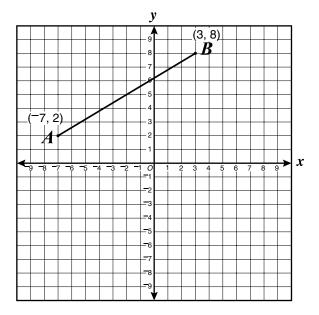
39 When standing upright, Gary knows his eyes are 6 feet above ground level. To determine the depth of a well, he stands in the position shown.



Using the given measures, how deep is the well?

- **A** 12 ft
- **B** 14 ft
- c 16 ft
- **D** 18 ft

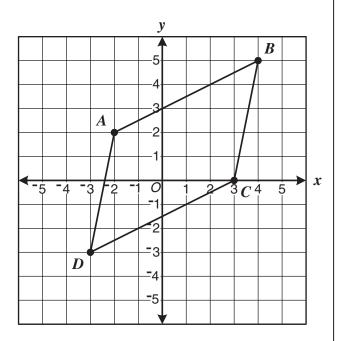
40



The coordinates of the midpoint of \overline{AB} are —

- **F** (5, 3)
- G (-5, 3)
- \mathbf{H} (2, 5)
- J (-2, 5)

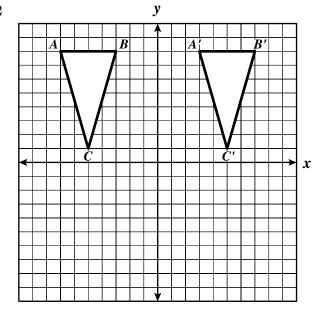
41 Parallelogram *ABCD* is placed on a coordinate grid as shown.



What is the approximate length of diagonal \overline{AC} ?

- A 3.0 units
- **B** 5.4 units
- c 9.0 units
- **D** 10.6 units

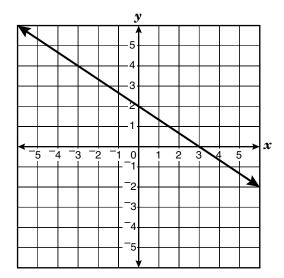
42



Triangle A'B'C' is —

- F a translation of triangle ABC across the v-axis
- ${f G}$ a 90° clockwise rotation of triangle ABC about the origin
- ${f H}$ a reflection of triangle ABC across the y-axis
- ${f J}$ a reflection of triangle ABC across the x-axis

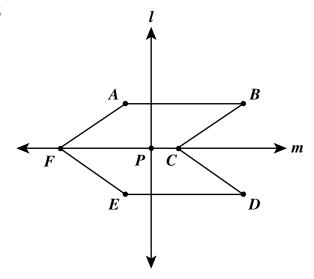
- 43 How many different lines of symmetry does a square have?
 - **A** 1
 - **B** 2
 - **C** 3
 - **D** 4



Which is most likely the slope of the line graphed?

- \mathbf{F} $^{-4}$
- $G = \frac{3}{5}$
- $\mathbf{H} = \frac{2}{3}$
- **J** 4

- 15 —



$\begin{array}{l} {\bf Hexagon} \ ABCDEF \ {\bf is \ apparently} \\ {\bf symmetric \ with \ respect \ to \ --} \end{array}$

- \mathbf{A} point P only
- **B** line m only
- \mathbf{C} line l only
- \mathbf{D} both lines l and m only

Answer Key

Test Sequence Number	Correct Answer	Reporting Category	Reporting Category Description
1	B	001	Lines and Angles
2	Н	001	Lines and Angles
3	В	001	Lines and Angles
4	F	001	Lines and Angles
5	В	001	Lines and Angles Lines and Angles
6	H	001	Lines and Angles
7	C	001	Lines and Angles
8	J	001	Lines and Angles
9	C	001	Lines and Angles
10	Н	001	Lines and Angles
11	В	001	Lines and Angles
12	F	002	Triangles and Logic
13	C	002	Triangles and Logic Triangles and Logic
14	G	002	Triangles and Logic Triangles and Logic
15	В	002	Triangles and Logic Triangles and Logic
16	F	002	Triangles and Logic
17	C	002	Triangles and Logic
18	J	002	Triangles and Logic
19	D	002	Triangles and Logic
20	J	002	Triangles and Logic
21	B	002	Triangles and Logic
22	G	002	Triangles and Logic
23	C	002	Triangles and Logic
24	Н	003	Polygons and Circles
25	A	003	Polygons and Circles
26	J	003	Polygons and Circles
27	C	003	Polygons and Circles
28	J	003	Polygons and Circles
29	D	003	Polygons and Circles
30		003	Polygons and Circles
31	C	003	Polygons and Circles
32	Н	003	Polygons and Circles
33	В	003	Polygons and Circles
34	 Ј	003	Three-Dimensional Figures
35	В	004	Three-Dimensional Figures Three-Dimensional Figures
36	G	004	Three-Dimensional Figures Three-Dimensional Figures
37	A A	004	Three-Dimensional Figures Three-Dimensional Figures
38	F	004	Three-Dimensional Figures Three-Dimensional Figures
39	 D	004	Three-Dimensional Figures Three-Dimensional Figures
40	J	005	Coordinate Relations and Transformations
			Coordinate Relations and Transformations Coordinate Relations and Transformations
41	В 	005	Coordinate Relations and Transformations Coordinate Relations and Transformations
42		005	Coordinate Relations and Transformations Coordinate Relations and Transformations
43	D	005	
44	H	005	Coordinate Relations and Transformations
45	В	005	Coordinate Relations and Transformations